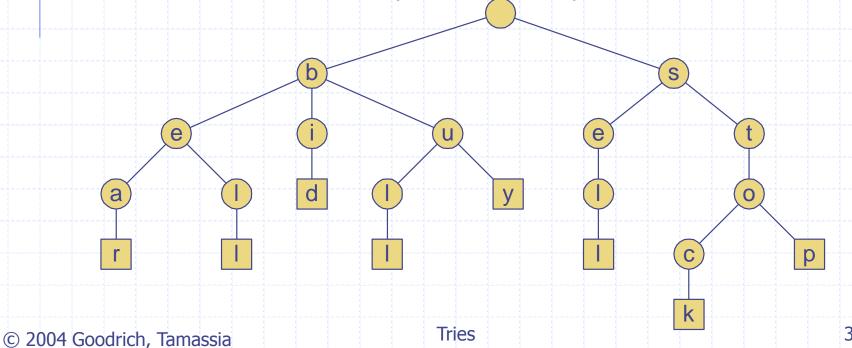


## Preprocessing Strings

- Preprocessing the pattern speeds up pattern matching queries
  - After preprocessing the pattern, KMP's algorithm performs pattern matching in time proportional to the text size
- If the text is large, immutable and searched for often (e.g., works by Shakespeare), we may want to preprocess the text instead of the pattern
- A trie is a compact data structure for representing a set of strings, such as all the words in a text
  - A tries supports pattern matching queries in time proportional to the pattern size

#### Standard Tries

- The standard trie for a set of strings S is an ordered tree such that:
  - Each node but the root is labeled with a character
  - The children of a node are alphabetically ordered
  - The paths from the external nodes to the root yield the strings of S
- Example: standard trie for the set of strings
  S = { bear, bell, bid, bull, buy, sell, stock, stop }

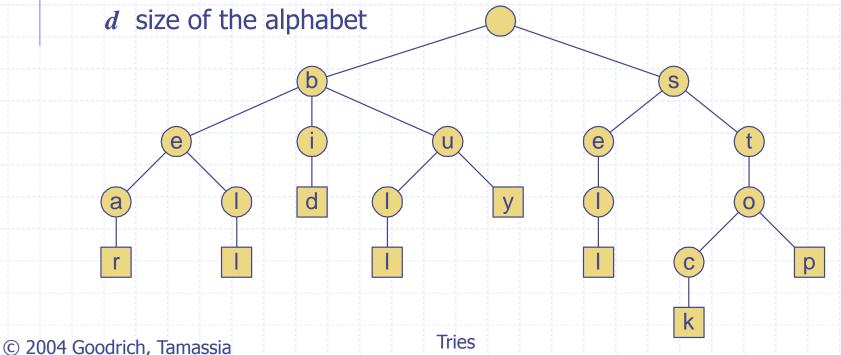


### **Analysis of Standard Tries**

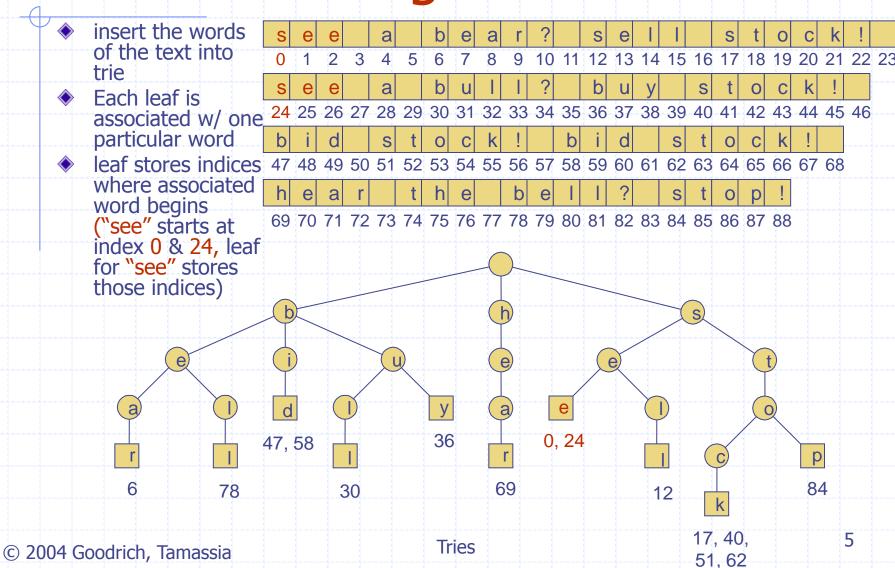
\* A standard trie uses O(n) space and supports searches, insertions and deletions in time O(dm), where:

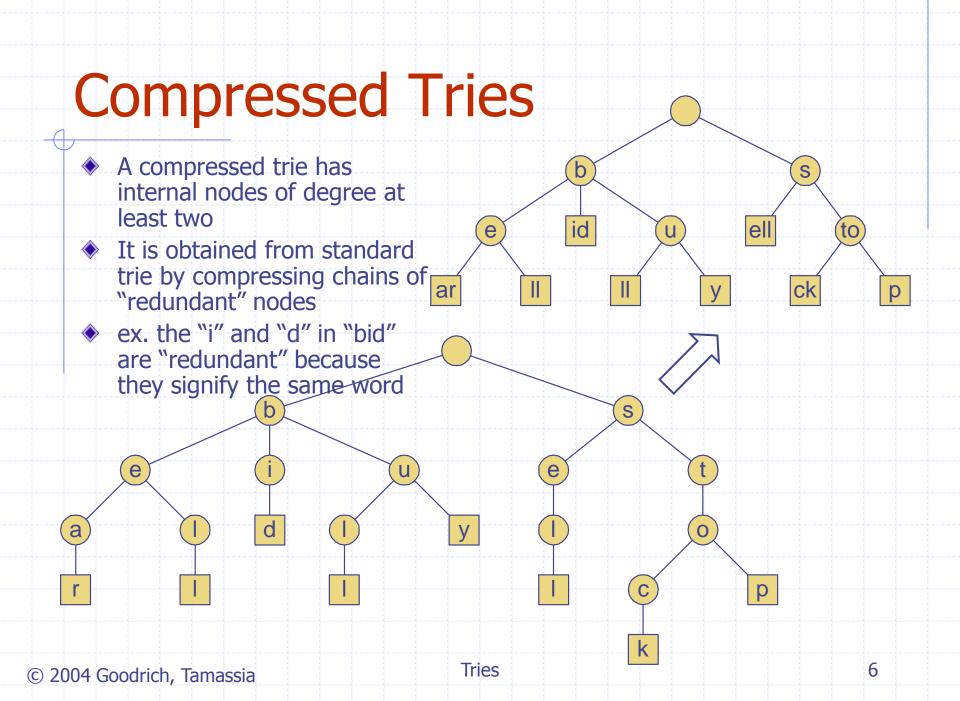
n total size of the strings in S

m size of the string parameter of the operation



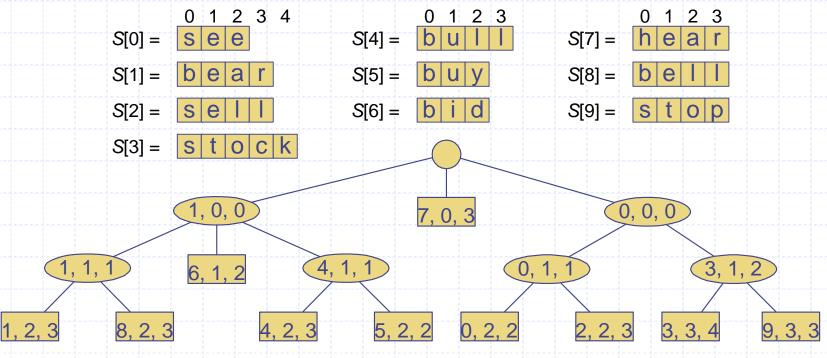
## Word Matching with a Trie





#### **Compact Representation**

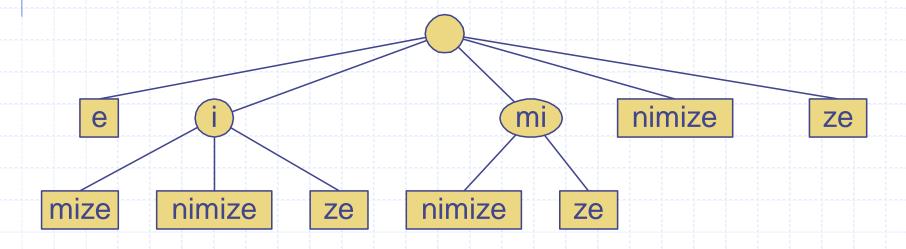
- Compact representation of a compressed trie for an array of strings:
  - Stores at the nodes ranges of indices instead of substrings
  - Uses O(s) space, where s is the number of strings in the array
  - Serves as an auxiliary index structure



#### Suffix Trie

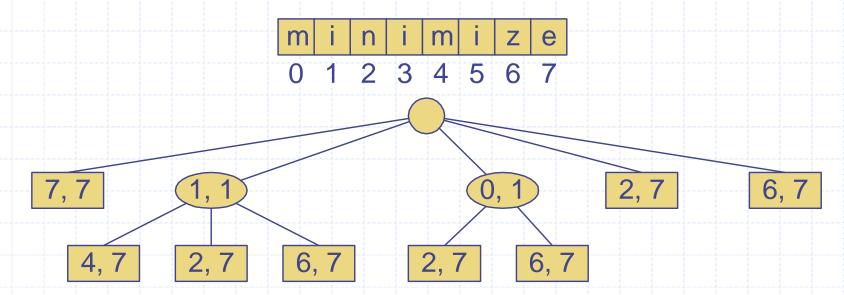
◆ The suffix trie of a string X is the compressed trie of all the suffixes of X





#### **Analysis of Suffix Tries**

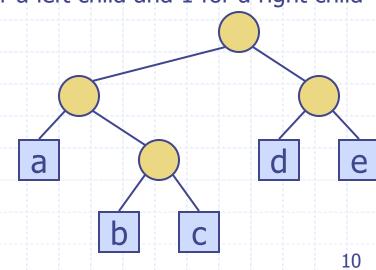
- lacktrianglet Compact representation of the suffix trie for a string X of size n from an alphabet of size d
  - Uses O(n) space
  - Supports arbitrary pattern matching queries in X in O(dm) time, where m is the size of the pattern
  - Can be constructed in O(n) time



## Encoding Trie (1)

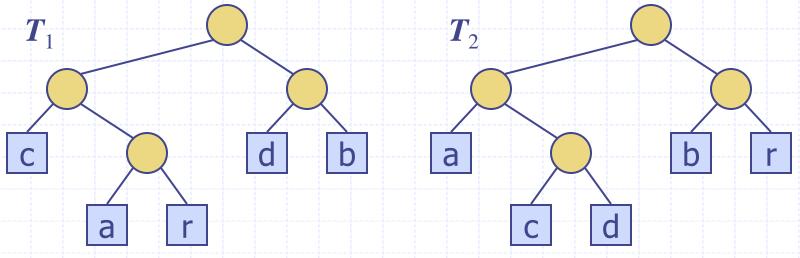
- A code is a mapping of each character of an alphabet to a binary code-word
- A prefix code is a binary code such that no code-word is the prefix of another code-word
- An encoding trie represents a prefix code
  - Each leaf stores a character
  - The code word of a character is given by the path from the root to the leaf storing the character (0 for a left child and 1 for a right child

00	010	011	10	11
a	b	С	d	е



## Encoding Trie (2)

- Given a text string X, we want to find a prefix code for the characters of X that yields a small encoding for X
  - Frequent characters should have short code-words
  - Rare characters should have long code-words
- Example
  - $\blacksquare$  X = abracadabra
  - $T_1$  encodes X into 29 bits
  - T<sub>2</sub> encodes X into 24 bits



### Huffman's Algorithm

- Given a string X, Huffman's algorithm construct a prefix code the minimizes the size of the encoding of X
- It runs in time  $O(n + d \log d)$ , where n is the size of Xand d is the number
  of distinct characters
  of X
- A heap-based priority queue is used as an auxiliary structure

```
Algorithm HuffmanEncoding(X)
  Input string X of size n
  Output optimal encoding trie for X
  C \leftarrow distinctCharacters(X)
  computeFrequencies(C, X)
  Q \leftarrow new empty heap
  for all c \in C
     T \leftarrow new single-node tree storing c
     Q.insert(getFrequency(c), T)
  while Q.size() > 1
     f_1 \leftarrow Q.min()
     T_1 \leftarrow Q.removeMin()
     f_2 \leftarrow Q.min()
     T_2 \leftarrow Q.removeMin()
     T \leftarrow join(T_1, T_2)
     Q.insert(f_1 + f_2, T)
  return Q.removeMin()
```

# Example

X = abracadabraFrequencies

a	b	C	d	r
5	2	1	1	2

